

الامتحان الثاني

تفاضل وتكامل (1)

Circle the correct answer (1.5 points each).

(1) $\log_{100} x + \log_{0.1} x = 1 \Rightarrow x =$

- (a) 0.01 (b) 1
(c) 100 (d) 0.1

(2) $f(x) = \tan x \Rightarrow (f^{-1})(\sqrt{3}) =$

- (a) dose not exist (b) $\sqrt{3}/2$
(c) $-\pi/6$ (d) $3/4$

(3) The curve $f(x) = x^2 - 6x^{1/3}$ has a vertical tangent at $x =$

- (a) 2 (b) 0
(c) 1 (d) 3

(4) $g(1) = 2, f'(2) = 3$ and $(f \circ g)'(1) = 4 \Rightarrow$

- $g'(1) =$
(a) 4 (b) $4/3$
(c) $3/4$ (d) 3

(5) The equation of the tangent line to the curve $y^4 - 2x^2 y^3 - 27 = 0$ at $(-1, 3)$ is

- (a) $y = -2x - 1$ (b) $y = -2x$
(c) $y = -2x + 1$ (d) $y = 2x - 1$

(6) $y = \sqrt[3]{\frac{x(x^2-1)}{(x-1)^2}} \Rightarrow y'|_{x=2} =$

- (a) $\sqrt[3]{5}/18$ (b) $\sqrt[3]{5}/18$
(c) ∞ (d) 0

(7) $y = (\ln x)^{\ln x} \Rightarrow y'|_{x=2} =$

- (a) e (b) e^{-1}
(c) 1 (d) 0

(8) $\lim_{x \rightarrow 0} \frac{4^{\sin x} - 1}{8^{\tan x} - 1} =$

- (a) $1/2$ (b) 0
(c) ∞ (d) does not exist

(9) $\lim_{x \rightarrow 0^+} \frac{\sin(\frac{1}{x})}{\sin x} =$

- (a) 1 (b) 0

(c) does not exist (d) ∞

(10) $\ln\left(1+\frac{1}{10}\right)+\ln\left(1+\frac{1}{11}\right)+\ln\left(1+\frac{1}{12}\right)+\dots+\ln\left(1+\frac{1}{29}\right)=$

- (a) 3 (b) 30
(c) $\ln 3$ (d) $\ln 30$

(1) Given $f(x)=x^{2/3}$, $a=-1$, $b=8$

(2points) (c) Show there is No $c \in (a,b)$:

$$f'(c)=\frac{f(b)-f(a)}{b-a}$$

(2points) (d) Explain this does not violate the mean value theorem.

(2) Given $f(x) = x^{5/3} - 5x^{2/3}$

(2points) (c) find all max, min, inflection points and cusps if any

(1points) (d) find intervals where function is increasing or decreasing

(1points) find intervals where function is concave up or down

(2points) (e) Sketch the graph of f.

Q1) Find all vertical and horizontal asymptotes for the graph

Of $f(x) = \frac{2x^2+5x+2}{x^2+2x}$

Q2) If $\frac{d}{dx}[f(x^2)] = X^2$ find $f'(x)$

Q3) let $f(x) = \sqrt{x^2+5}$. Find $g(x)$ so that $g'(x) = f'(x)$ $g(-2) = 5$

Q4) let $x^2 - xy + y^2 = 10$ find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$

At the point (1,1)