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a) Sketch the root locus given by $G(s)H(s) = \frac{K(s^2 - 4s + 8)}{(s^2 + 2s + 2)(s + 4)}$

If two roots on the locus are pure imaginary, outline how you would find the third root **graphically**. Formulate any equation needed without solving it.

b) For the unity feedback system with open loop transfer function as in part (a) : Obtain **graphically** the closed loop unit step time response for the case where the closed loop poles are approximated by $\pm 2j$ and -6 at $k = k_c$.

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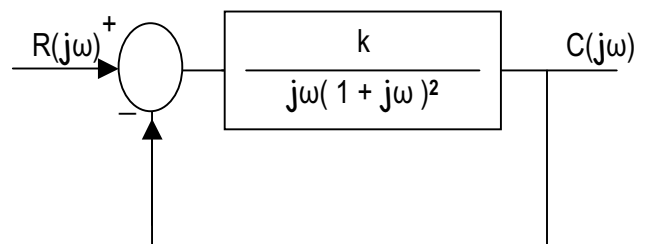
a) Sketch the asymptotic Bode diagram of $G(j\omega)$ as $\frac{(1 - \omega/4)}{j\omega(1 + j\omega/2)}$

Hence, find the gain margin **using the diagram**.

b) Given the system shown :

* For $k = 1$, plot the Nyquist diagram using the information at $\omega = 0.8$ rad/sec and $\omega = 0.9$ rad/sec together with the information that the gain margin is 2 and that the phase margin is $90 - 2 \tan^{-1} 0.7$.

Using graphical methods.



* Find the steady state time output $c(t)$ when $k = 1.4$ and when $k = 3$ and the input is $r(t) = 5 \sin(\omega t)$.

* Find the value of k such that the maximum closed loop magnitude due to a unit sinusoid is 1.5.